

Opgave 1 :

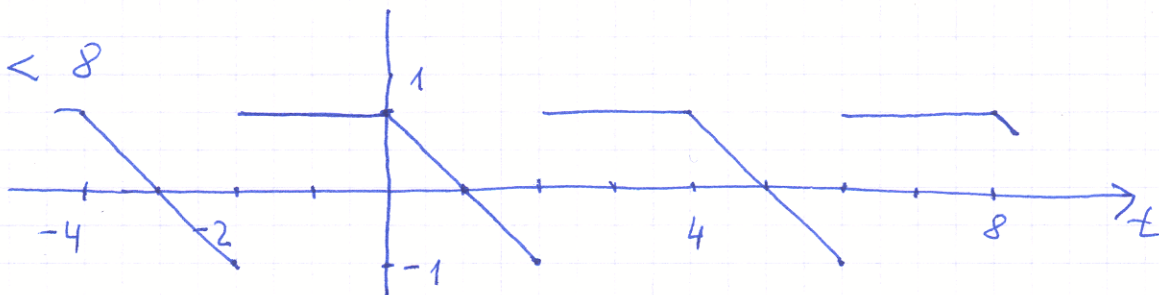
Løsningsforslag

I2SIG1/maj 01/DP

$T=4$

$$f(t) = \begin{cases} 1 & \text{for } -\frac{T}{2} < t < 0 \\ 1-t & \text{for } 0 < t < \frac{T}{2} \end{cases}$$

a)  $-4 < t < 8$



b) funktionen er hverken lige eller ulige, fordi

$$f(t) \neq \pm f(-t) \quad f(-1) = 1 \quad f(1) = 0 \Rightarrow f(-1) \neq f(1)$$

$$\omega_1 = \frac{2\pi}{T} = \frac{2\pi}{4} = \frac{\pi}{2}$$

$$c) a_0 = \frac{2}{T} \left( \int_{-2}^0 1 dt + \int_0^2 (1-t) dt \right) = \frac{1}{2} \left( t \Big|_{-2}^0 + \left( t - \frac{1}{2}t^2 \right) \Big|_0^2 \right)$$

$$a_0 = \frac{1}{2} (2 + 2 - 2) = \underline{1}$$

$$d) a_n = \frac{2}{4} \left( \int_{-2}^0 1 \cdot \cos\left(\frac{\pi}{2}nt\right) dt + \int_0^2 (1-t) \cos\left(\frac{\pi}{2}nt\right) dt \right)$$

$$b_n = \frac{2}{4} \left( \int_{-2}^0 1 \cdot \sin\left(\frac{\pi}{2}nt\right) dt + \int_0^2 (1-t) \sin\left(\frac{\pi}{2}nt\right) dt \right)$$

$$a_n = \begin{cases} \frac{4}{n^2\pi^2} & \text{for } n \text{ ulige} \\ 0 & \text{for } n \text{ lige} \end{cases} \quad b_n = \frac{2}{n\pi} (-1)^n$$

$$e) f(t) \approx \frac{1}{2} + \frac{4}{\pi^2} \cos \frac{\pi}{2}t - \frac{2}{\pi} \sin \frac{\pi}{2}t + \frac{1}{\pi} \sin \pi t + \frac{4}{9\pi^2} \cos \frac{3\pi}{2}t - \frac{2}{3\pi} \sin \frac{3\pi}{2}t$$

$$f) \text{ t Collect } \left( \frac{4}{\pi^2} \cos \left( \frac{\pi}{2}t \right) - \frac{2}{\pi} \sin \left( \frac{\pi}{2}t \right) \right) = \frac{2\sqrt{\pi^2+4}}{\pi^2} \cos \left( \frac{\pi}{2}t + 1,004 \right)$$

$$\text{t Collect } \left( \frac{4}{9\pi^2} \cos \left( \frac{3\pi}{2}t \right) - \frac{2}{3\pi} \sin \left( \frac{3\pi}{2}t \right) \right) = \frac{2\sqrt{9\pi^2+4}}{9\pi^2} \cos \left( \frac{3\pi}{2}t + 1,362 \right)$$

$$f(t) \approx \frac{1}{2} + \frac{2\sqrt{\pi^2+4}}{\pi^2} \cos \left( \frac{\pi}{2}t + 1,004 \right) + \frac{1}{\pi} \cos \left( \pi t - \frac{\pi}{2} \right) + \frac{2\sqrt{9\pi^2+4}}{9\pi^2} \cos \left( \frac{3\pi}{2}t + 1,362 \right)$$