

s. 728 Ex 1

Half-range sine series:

$$f(t) = t \sin t \quad 0 \leq t \leq \pi \quad T = 2\pi \quad \omega = 1$$

$a_0 = 0, a_n = 0$  for  $n$  positive here tal

$$b_n = \frac{4}{2\pi} \int_0^{\pi} t \sin t \sin nt \, dt = \left( \frac{1}{(n+1)^2\pi} - \frac{1}{(n-1)^2\pi} \right) \cos(n\pi) + \left( \frac{1}{n+1} - \frac{1}{n-1} \right) \sin(n\pi) + \frac{1}{(n+1)^2\pi} - \frac{1}{(n-1)^2\pi}$$

$n \neq 1$

$$= \left( \frac{1}{(n+1)^2\pi} - \frac{1}{(n-1)^2\pi} \right) \left( (-1)^n + 1 \right) = \frac{(n-1)^2 - (n+1)^2}{(n-1)^2(n+1)^2\pi} \left( (-1)^n + 1 \right)$$

$$b_n = \frac{-4n \cdot ((-1)^n + 1)}{(n-1)^2(n+1)^2\pi}$$

$$b_1 = \frac{4}{2\pi} \int_0^{\pi} t \sin t \cdot \sin t \, dt = \frac{\pi}{2}$$

$$f(t) = \frac{\pi}{2} \sin t + \sum_{n=2}^{\infty} \frac{-4n((-1)^n + 1)}{(n-1)^2(n+1)^2\pi} \sin(nt)$$

$$f(t) := \frac{\pi}{2} \sin(t) + \sum_{n=2}^{10} -4 \cdot n \cdot \frac{(-1)^n + 1}{(n-1)^2 \cdot (n+1)^2 \cdot \pi} \cdot \sin(n \cdot t)$$

